

OPENER

a) What is the slope of the line that goes through A(5, -2) and B (3, 6)

$$\text{Recall } m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-2 - 6}{5 - 3} = \frac{-8}{2}$$

$$m = -4$$

b) What is the equation of that line?

$$y = mx + b$$

$$-2 = -4(5) + b$$

$$-2 = -20 + b$$

$$18 = b$$

$$y = -4x + 18$$

Continuing Midpoint questions

$5 + (-3)$

ex1: A triangle has the vertices at A (-3, -1), B (3, 5) and C (7, -3).
Determine the equation of the median from vertex A.

① $M_{BC} = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$
 $= \left(\frac{3+7}{2}, \frac{5+(-3)}{2} \right)$
 $= \left(\frac{10}{2}, \frac{2}{2} \right)$
 $M_{BC} = (5, 1)$

② $m_{AD} = \frac{y_2 - y_1}{x_2 - x_1}$
 $= \frac{1 - (-1)}{5 - (-3)}$
 $= \frac{2}{8}$
 $m_{AD} = \frac{1}{4}$

$\left. \begin{array}{l} \frac{-1 - 1}{-3 - 5} \\ = \frac{-2}{-8} \\ = \frac{1}{4} \end{array} \right\}$

③ $y = \frac{1}{4}x + b$ using D(5, 1)

$$1 = \frac{1}{4}(5) + b$$

$$1 = \frac{5}{4} + b$$

$$1 - \frac{5}{4} = b$$

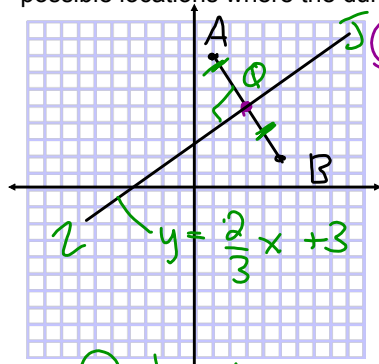
$$-\frac{1}{4} = b$$

∴ equation of
the median from

A is $y = \frac{1}{4}x - \frac{1}{4}$

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ex2: A dumpster need to be put at equal distances between two buildings which are located at A(1, 8) and B(5, 2). Describe all possible locations where the dumpster might be located.



① M_{AB} is one location!

$$M_{AB} = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

$$= \frac{1+5}{2}, \frac{8+2}{2}$$

$$M_{AB} = 3, 5$$

② Need perpendicular bisector equation - don't have 2 pts on ZJ \therefore need to use M_{AB}

$$\begin{aligned} m_{AB} &= \frac{y_2 - y_1}{x_2 - x_1} \\ &= \frac{8 - 2}{1 - 5} \\ &= \frac{6}{-4} \\ &= -\frac{3}{2} \end{aligned}$$

$$\therefore m_{ZJ} = \frac{2}{3}$$

③ solve for b using $M_{AB} = (3, 5)$

$$y = \frac{2}{3}x + b$$

$$5 = \frac{2}{3}(3) + b$$

$$5 = 2 + b$$

$$3 = b$$

$$y = \frac{2}{3}x + 3$$

Therefore to find a point on the line where the dumpster can be located, choose a value of x . then solve for y
if $x = -6$, $y = ?$

$$y = \frac{2}{3}(-6) + 3$$

$$y = -\frac{12}{3} + 3$$

$$y = -4 + 3$$

$$y = -1$$

In Summary: to find the perpendicular bisector of two points you do the following

1 - Find the Midpoint of the original points

2 - Find the slope of the original points

3 - You can now get the slope of the perpendicular bisector by creating the negative reciprocal of the slope you calculated

4 - Find the y-int of the perpendicular bisector by substituting known slope and Midpoint values for (x, y) .

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